# Discussion of 'A Multisector Perspective on Wage Stagnation' by L. Rachel Ngai and Orhun Sevinc

Zsófia L. Bárány

Sciences Po and CEPR

2019 December, Frankfurt ECB-CEPR Labour Market Workshop

## Summary

Wage decoupling & low-skill wage stagnation well known. This paper: Look at low-skill wage divergence (decoupling).

Empirical decomposition:

$$\frac{\text{labour productivity}}{\text{real low-sk wage}} = \frac{y/P_Y}{w_l/P_C} = \frac{P_C}{P_Y}\frac{y}{w_l} = \frac{P_C}{P_Y}\frac{\frac{w}{\beta}}{w_l} = \frac{P_C}{P_Y}\frac{w}{w_l}\frac{1}{\beta}$$

• 
$$\frac{P_C}{P_Y}$$
 – cost of living

- $\frac{y}{w_i}$  nominal divergence
  - \*  $\frac{w}{w_l}$  wage inequality \*  $\beta$  labour income share
- Propose a mechanism:
  - Augment standard structural change model.
  - + Nested CES of K, H, L with diff & changing intensities across sectors.
  - + K and H complements, both are good substitutes for L.
  - + ST comes from: TFP growth diff across sectors & falling price of K.

#### Olibrate to gauge magnitudes.

Decompose

real divergence

into the contribution of

- increasing living costs
- increasing inequality
- decreasing labour share

Decompose

real divergence

increasing over time

into the contribution of

- increasing living costs
- increasing inequality
- decreasing labour share

Decompose

• real divergence increasing over time

into the contribution of

- increasing living costs
- increasing inequality
- decreasing labour share

positive, decreasing, average: 30%

Decompose

• real divergence increasing over time

into the contribution of

- increasing living costs
- increasing inequality
- decreasing labour share

positive, decreasing, average: 30% positive, fluctuates, average: 49%

Decompose

• real divergence increasing over time

into the contribution of

- increasing living costs
- increasing inequality
- decreasing labour share

positive, decreasing, average: 30% positive, fluctuates, average: 49% pos/neg, fluctuates, average: 21%

## The model in a nutshell

• output 
$$j = G, S$$
:  

$$Y_{j} = A_{j} \left[ \xi_{j} L_{j}^{\frac{\eta-1}{\eta}} + (1 - \xi_{j}) \left[ \kappa_{j} K_{j}^{\frac{\rho-1}{\rho}} + (1 - \kappa_{j}) H_{j}^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1} \frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

- $P_j$  equals the marginal cost of production
- labour market: exogenous *H* and *L*

wage equalisation across sectors

- $C_g$  and  $C_s$  chosen to maximise homothetic utility, elasticity arepsilon < 1
- market clearing:  $Y_s = C_s$  and  $Y_g = C_g + \phi K$
- $\rightarrow$  Question: is K determined as a residual from accounting identity?

Exogenously changing:

- skill supply: *H*, *L*
- sectoral TFP: A<sub>g</sub>, A<sub>s</sub>
- price of capital:  $\phi$
- production "weights":  $\xi_g, \xi_s, \kappa_g, \kappa_s$

# Mechanism 1: Structural Transformation

- output 
$$j = G, S$$
:  

$$Y_{j} = A_{j} \left[ \xi_{j} L_{j}^{\frac{\eta-1}{\eta}} + (1 - \xi_{j}) \left[ \kappa_{j} K_{j}^{\frac{\rho-1}{\rho}} + (1 - \kappa_{j}) H_{j}^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1}\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

- $P_j$  equals the marginal cost of production
- labour market: exogenous H and L

wage equalisation across sectors

- $\mathit{C_g}$  and  $\mathit{C_s}$  chosen to maximise homothetic utility, elasticity  $\varepsilon < 1$
- market clearing:  $Y_s = C_s$  and  $Y_g = C_g + \phi K$

Assumptions:

#### $\varepsilon < 1$ & $A_g \uparrow > A_s \uparrow$ (Ngai and Pissarides 2007)

Mechanism:

1. G more productive  $\Rightarrow$  ceteris paribus  $Y_g/Y_s \uparrow \& P_g/P_s \downarrow$ demand for G goes up, but less than supply would due to  $\varepsilon < 1$  $\Rightarrow$  inputs reallocate towards S

2. increasing  $P_s/P_g$  & K comes from  $Y_g$   $\Rightarrow$  rising relative cost of living

## Mechanism 2: Skill biased ST

- output 
$$j = G, S$$
:  

$$Y_{j} = A_{j} \left[ \xi_{j} L_{j}^{\frac{\eta-1}{\eta}} + (1 - \xi_{j}) \left[ \kappa_{j} K_{j}^{\frac{\rho-1}{\rho}} + (1 - \kappa_{j}) H_{j}^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1} \frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

- $P_j$  equals the marginal cost of production
- labour market: exogenous H and L

wage equalisation across sectors

- $C_g$  and  $C_s$  chosen to maximise homothetic utility, elasticity arepsilon < 1
- market clearing:  $\mathit{Y_s} = \mathit{C_s}$  and  $\mathit{Y_g} = \mathit{C_g} + \phi \mathit{K}$

Assumptions:

$$arepsilon < 1$$
 &  $A_g \uparrow > A_s \uparrow$  &  $\xi_g > \xi_s$  (Buera et al. 2018)

Mechanism:

inputs move to S, which more intensive in  $H \Rightarrow$  demand for  $H/L \uparrow \Rightarrow$  skill premium  $\uparrow$ 

# Mechanism 3: Capital-skill complementarity

output 
$$j = G, S$$
:  

$$Y_{j} = A_{j} \left[ \xi_{j} L_{j}^{\frac{\eta-1}{\eta}} + (1 - \xi_{j}) \left[ \kappa_{j} K_{j}^{\frac{\rho-1}{\rho}} + (1 - \kappa_{j}) H_{j}^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1} \frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

- $P_j$  equals the marginal cost of production
- labour market: exogenous H and L wage equalisation across sectors
- $\mathit{C_g}$  and  $\mathit{C_s}$  chosen to maximise homothetic utility, elasticity  $\varepsilon < 1$
- market clearing:  $Y_s = C_s$  and  $Y_g = C_g + \phi K$

Assumptions:

 $\eta > 1 > \rho$  &  $\phi \downarrow$  (Krusell et al. 2000)

Mechanism:

1.  $\phi \downarrow \Rightarrow$  more K, complements H and substitutes  $L \Rightarrow$  skill premium  $\uparrow$ 2.  $\kappa_g > \kappa_s$  and  $K \uparrow \Rightarrow G$  output grows faster  $\Rightarrow$  ST

#### Calibration: 1980-2003

Calibration strategy largely follows Buera et al. (2018):

- $\varepsilon, \eta, \rho$ : elasticities taken off the shelf
- $\gamma_{A_g}, \gamma_{A_s}, \gamma_{\phi}$ : calibrated to match  $\Delta$  in  $P_g/P_s$ , relative price of capital, aggregate lab prod growth
- $\xi_{g,t}, \xi_{s,t}, \kappa_{g,t}, \kappa_{s,t}, H_t/L_t$ : calibrated to match income share of factors (K, H, L) within sectors, and overall income share of H and L
- $\rightarrow\,$  How is the weight in the utility function calibrated? To match value added shares?

## Quantification: 1980-2003

Model

- reproduces 75% of real divergence
- relative role of change in living costs, inequality and labour share in line with decomposition

Quantify importance of each channel by shutting down the rest:

- $\gamma_{A_g} > \gamma_{A_s}$ : 1/3 of real div, half through living costs, but lab share  $\uparrow$
- $\gamma_{\phi} <$  1: 1/4 of real div, almost all through inequality, but lab share  $\uparrow$
- $\xi_j, \kappa_j \downarrow$ : 55% of real div, 3/4 inequality, 1/4 labour share
- H/L  $\uparrow$ : suppresses real div, but reduces lab share

 $\rightarrow$  Points to interaction between channels.

#### What is new in this paper?

- Model and calibration basically identical to Buera et al. (2018), with the addition of capital (as in Krusell et al. (2000))
- The question is different:
  - Buera et al: skill premium
  - this paper: divergence and its components
    - 1. inequality (very related to skill premium)
    - 2. labour share
    - 3. cost of living
    - $\rightarrow$  2. and 3. cannot be studied without capital

## What do we learn from this paper?

- Empirical decomposition of low skilled wage divergence into inequality, labour share and cost of living.
   → I find this very interesting.
- 2. Why do we want a model with three mechanisms that delivers all three components jointly?

It could be that each of these is driven by different mechanisms.

 $\rightarrow$  However, model shows that each mechanism connects some components.

- ► Diff sectoral TFP growth generates inequality and rising costs of living.
- Changing "weights" generate inequality and decline in labour share.
- ► Falling capital cost and changing capital "weights" less important.

### Comments - Changing factor weights

• What do changes in the weights of various production factors mean?

$$Y_{j,t} = A_{j,t} \left[ \xi_{j,t} L_{j,t}^{\frac{\eta-1}{\eta}} + (1-\xi_{j,t}) \left[ \kappa_{j,t} K_{j,t}^{\frac{\rho-1}{\rho}} + (1-\kappa_{j,t}) H_{j,t}^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1}\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

A<sub>j,t</sub> – between sector skill biased demand shift

•  $\xi_{j,t}$  – within sector skill biased demand shift

## Comments - Changing factor weights

• What do changes in the weights of various production factors mean?

$$Y_{j,t} = A_{j,t} \left[ \xi_{j,t} L_{j,t}^{\frac{\eta-1}{\eta}} + (1 - \xi_{j,t}) \left[ \kappa_{j,t} K_{j,t}^{\frac{\rho-1}{\rho}} + (1 - \kappa_{j,t}) H_{j,t}^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1}\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

A<sub>j,t</sub> – between sector skill biased demand shift

- $\xi_{j,t}$  within sector skill biased demand shift
- Equivalent to sector-specific factor-augmenting technologies.

$$Y_{j,t} = \left[ \left( Z_{jL,t} L_{j,t} \right)^{\frac{\eta-1}{\eta}} + \left[ \left( Z_{jK,t} K_{j,t} \right)^{\frac{\rho-1}{\rho}} + \left( Z_{jH,t} H_{j,t} \right)^{\frac{\rho-1}{\rho}} \right]^{\frac{\rho}{\rho-1} \frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

- Normalising the changing weights is not innocuous. ⇒ The distinction of *between sector* and *within sector* demand shifts hinges on this.
- Alternative: calibrate sector-specific factor-augmenting technologies
   → extract sector and factor components from these (Bárány and
   Siegel (2019a)).

## Comments - Low vs high-skilled labour

- Understanding the drivers of low-skilled wage growth is important.
- Here: model low- and high-skilled labour as different factors of production.
  - Equivalent to high-skilled having different jobs than low-skilled.
- Alternative production function: occupational labour as diff inputs.
  - The mapping from education to occupations is not unique and is changing.
  - In particular composition of occupations among the low-skilled have changed and contributed to wage stagnation.

#### Comments

- Definition of sectors.
  - Makes sense from the production side.
  - Not justified from the consumption side. All industries within 'Goods' are perfect substitutes.
- Look at sub-periods.
  - Marked changes in relative role of cost of living, inequality, and labour share.
  - Could check whether the evolution of model implied sources, φ, changing weights, sectoral TFP are in line with this timing.

## Summary

- Very interesting paper.
- Key novelty: Empirical decomposition and its connection to the various channels in the model.
  - Could be further developed by looking at sub-periods.
  - Consider looking at occupations.
  - Distinction of between- and within-industry shifters.