#### Labor force participation, wage rigidities, and inflation

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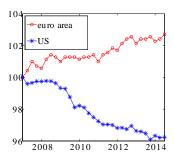
#### Challenges for macroeconomic policy in a low inflation environment ECB 5-6 November 2015

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#### Motivation

▶ LFP

ECB, Economic Bulletin, 1-2015 "Despite the severe recessionary periods that have affected the euro area in recent years, the labour force participation rate in the euro area has shown atypically positive developments."



Labor force participation rate, Aged 15-64

US, OECD; euro area: Labor Force Survey (Eurostat). Euro area data refer to the EA-18 aggregate

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• YELLEN (2014): "...the key question is: What portion of the decline in LFP reflects structural shifts and what portion reflects cyclical weakness in the labor market? [...] the pace of the decline (in LFP) accelerated with the recession [...] greater worker discouragement is most directly the result of a weak labor market...<u>The interaction of labor force participation</u> and inflationary pressures has been understudied"

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- ERCEG AND LEVIN (2014): "Our paper provides compelling evidence that cyclical factors account for the bulk of the recent decline in the LFP rate " Similar results in Van Zandweghe 2012; Hotchkiss and Rios-Avila 2013, among others.

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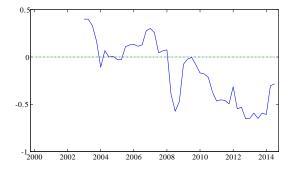
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  - Irrelevance of real wage rigidities for inflation

Rolling Correlations between hp-filtered LFP and gdp growth in the euro area



Correlations are calculated in a 3-year rolling window of quarterly data

LFP rate refers to the working age population (15-64)

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	hp-filtered LFP	
	<i>Post</i> 2008	<i>Post</i> 2000
Constant	-0.010 (0.036)	-0.027 (0.029)
$\frac{GDP_t - GDP_{t-1}}{GDP_{t-1}}$	$-0.088^{**}$ (0.043)	
$\frac{GDP_t - GDP_{t-1}}{GDP_{t-1}} * D_pre_2008$		-0.090 (0.062)
$\frac{GDP_t - GDP_{t-1}}{GDP_{t-1}} * D_post_2008$		$-0.090^{**}$ (0.041)

\*\* significance at the 5 per cent level.

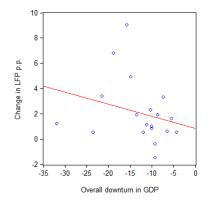
Panel regression

	Post 2008
	hp-filtered LFP
Constant	-0.015
	(0.031)
$\frac{GDP_{it} - GDP_{it-1}}{GDP_{it-1}}$	-0.048**
	(0.020)
**	

significance at the 5 per cent level.

Panel regression on euro area countries, where we control for cross-country heterogeneity by allowing for time-invariant, country-specific fixed effects in the estimation.

The increase in the labor force participation rate has been larger in those euro area countries that have been hit the hardest by the crisis



euro area 19

Notes: on the horizontal axis, we consider the difference between the lowest and the highest value of real GDP attained by each country in the post-2007

period. In the vertical axis the overall change in the LFP rate over the post-2007 period is considered,

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- What is new:

Standard business cycle models ignore the participation margin.

In our model household's labor supply choices include how many family members should participate in the market work, rather than contribute to home labor. Family members can be employed, unemployed (and searching for a job), or out of the labor force

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• We follow Campolmi and Gnocchi (2014) in modeling labor market flows

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#### ► Utility

The household allocates members to market production up to the point at which the marginal cost in terms of foregone home production equals the marginal return to market work:

$$\underbrace{\frac{\chi(1-N_{t})^{-\phi}}{\Omega_{t}}}_{MRS_{t,L,C}} = f_{t} \underbrace{\left(\frac{W_{t}}{P_{t}} - \underbrace{\frac{\psi E_{t}^{\varsigma}}{\Omega_{t}}}_{WRS_{E,C}}\right)}_{wage \ markup} + f_{t} \mathbb{E}_{t} \beta \left(1-\rho\right) \frac{\Omega_{t+1}}{\Omega_{t}} \frac{(1-f_{t+1})}{f_{t+1}} MRS_{t+1,L,C}$$

- $N_t$  : the pool of labor market participants
- $\Omega_t$  : marginal utility of consumption
- $f_t$ : the probability of being hired in period t
- $E_t$ : the mass of employed
- ho : the separation rate

$$\begin{split} \chi(1-N_{t})^{-\phi} &= \\ \Omega_{t}f_{t}\underbrace{\left(\frac{W_{t}}{P_{t}}-\frac{\psi E_{t}^{\varsigma}}{\Omega_{t}}\right)}_{\text{wage markup}} + f_{t}\mathbb{E}_{t}\beta\left(1-\rho\right)\frac{\Omega_{t+1}\xi_{t+1}}{\Omega_{t}\xi_{t}}\frac{(1-f_{t+1})}{f_{t+1}}MRS_{t+1,L,C} \end{split}$$



• discouragement effect: the fall in workers' chances of finding jobs  $f_t \downarrow$  and the worsening of real wages  $\frac{W_t}{P_t} \downarrow$  drive potential workers out of the labor force  $N_t \downarrow$  leading to a procyclical response of labor force participation, as in the US.

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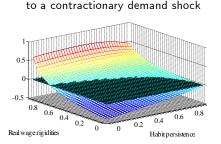
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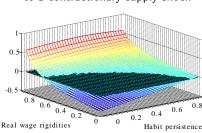
After a recessionary shock:

- discouragement effect: the fall in workers' chances of finding jobs  $f_t \downarrow$  and the worsening of real wages  $\frac{W_t}{P_t} \downarrow$  drive potential workers out of the labor force  $N_t \downarrow$  leading to a procyclical response of labor force participation, as in the US.
- <u>added worker effect</u>: when the degree of habit formation in strong (i.e. when household aspires to maintain its pre-crisis consumption level) and/or in the presence of high wage rigidities (preventing real wages from falling as much as reservation wages): family members might be prompted to seek jobs N<sub>t</sub> ↑, leading to a countercyclical profile of labor force participation, as in the euro area.

- Higher relevance of real wage rigidities in the euro area
- Differences in preferences: a higher degree of habit formation in the consumers' behavior in the euro area

Response at impact of labor market participation





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#### to a contractionary supply shock

• Two sectors: intermediate firms and retailers. Household's members are employed by intermediate firms - which face hiring costs and operate in a competitive market in relation to the goods they produce. Intermediate firms sell their output to retailers, which are monopolistically competitive and set prices in a staggered fashion (Calvo)

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$$MC_t = \underbrace{\frac{W_t}{P_t A_t}}_{\text{wage/productivity}} + \underbrace{Bf_t^{\eta}}_{\text{hiring costs}} - \underbrace{\beta \mathbb{E}_t \frac{\Omega_{t+1} \xi_{t+1}}{\Omega_t \xi_t} (1-\rho) \frac{A_{t+1}}{A_t} Bf_{t+1}^{\eta}}_{\text{reduced hiring needs}}$$

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• The job finding rate  $f_t$  - defined as the ratio of hires to the unemployment pool - is a measure of labor market tightness

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- The job finding rate  $f_t$  defined as the ratio of hires to the unemployment pool is a measure of labor market tightness
- Hiring costs are increasing with labor market tightness.

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$$\frac{W_t}{P_t} = \left(\frac{W_{t-1}}{P_{t-1}}\right)^{\gamma} (W_t^{r*})^{1-\gamma}$$

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$$\frac{W_t}{P_t} = \left(\frac{W_{t-1}}{P_{t-1}}\right)^{\gamma} (W_t^{r*})^{1-\gamma}$$
  
•  $W_t^{r*} = \frac{b\overline{W}_t^r}{firms reservation wage} + \frac{(1-b)\underline{W}_t^r}{wor \ker s opportunity cost of holding the job}$ 

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firms reservation wage workers opportunity cost of holding the job  
•  $\overline{W}_t^r = \frac{A_t}{\mu_t} + \beta \mathbb{E}_t \frac{\Omega_{t+1}}{\Omega_t} \frac{\xi_{t+1}}{\xi_t} (1-\rho) A_{t+1} B f_{t+1}^{\eta}$   
Sum of the marginal revenue product and the marginal saving on hiring costs  
resulting from the reduced hiring needs in t+1

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- $\frac{W_t}{P_t} = \left(\frac{W_{t-1}}{P_{t-1}}\right)^{\gamma} (W_t^{r*})^{1-\gamma}$   $W_t^{r*} = b\overline{W}_t^r + (1-b)\underline{W}_t^r$ firms reservation wage workers opportunity cost of holding the job
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    $\frac{W_t^r}{\Omega_t} \equiv \frac{\psi E_t^{\zeta}}{\Omega_t} \beta \mathbb{E}_t \frac{\Omega_{t+1}}{\Omega_t} \frac{\xi_{t+1}}{\xi_t} (1-\rho) S_{t+1}^H + \beta \mathbb{E}_t \frac{\Omega_{t+1}}{\Omega_t} \frac{\xi_{t+1}}{\xi_t} (1-\rho) f_{t+1} S_{t+1}^H$ 
  - Sum of labor disutility net of the discounted future surplus resulting from the employment relationship- and the value of searching for other jobs

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- <sup>W</sup><sub>t</sub> = (<sup>W</sup><sub>t-1</sub>)<sup>γ</sup> (W<sup>r\*</sup><sub>t</sub>)<sup>1-γ</sup>
   <sup>W</sup><sub>t</sub> = bW<sup>r</sup><sub>t</sub> + (1-b)W<sup>r</sup><sub>t</sub> firms reservation wage workers opportunity cost of holding the job
   <sup>W</sup><sub>t</sub> = A<sub>t</sub> + βE<sub>t</sub> Ω<sub>t+1</sub> ζ<sub>t+1</sub> ζ<sub>t+1</sub> (1-ρ) A<sub>t+1</sub>Bf<sup>η</sup><sub>t+1</sub> Sum of the marginal revenue product and the marginal saving on hiring costs resulting from the reduced hiring needs in t+1
   <sup>W</sup><sub>t</sub> = ψ<sup>E<sup>S</sup><sub>t</sub></sup>/Ω<sub>t</sub> - βE<sub>t</sub> Ω<sub>t+1</sub> ζ<sub>t+1</sub> ζ<sub>t+1</sub> (1-ρ) S<sup>H</sup><sub>t+1</sub> + βE<sub>t</sub> Ω<sub>t+1</sub> ζ<sub>t+1</sub> ζ<sub>t+1</sub> (1-ρ) f<sub>t+1</sub>S<sup>H</sup><sub>t+1</sub> Sum of labor disutility - net of the discounted future surplus resulting from the
- employment relationship- and the value of searching for other jobs
- $\overline{W}_t^r$  and  $\underline{W}_t^r$  are both increasing with labor market tightness: a tighter labor market increases both the workers outside option during the bargaining process (it is easier to find a job) and the firm's surplus from an employment relationship (it is more difficult to replace the worker).

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  - Conditional on adverse demand shocks: the drop in inflation will be shrunk by RWRs

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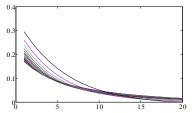
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  - Conditional on adverse supply shocks: the increase in inflation will be amplified by RWRs
  - Conditional on adverse demand shocks: the drop in inflation will be shrunk by RWRs
- When labor force cyclicality is considered, RWRs become irrelevant for inflation dynamics:

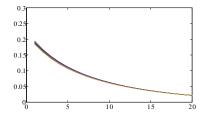
to the extent RWRs stimulate a countercyclical behavior of labor force, they leave roughly unchanged inflation.

IRFs of inflation to a recessionary supply shocks for different degrees of RWRs

Constant participation

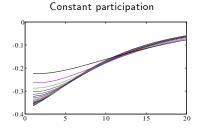
Endogenous participation





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IRFs of inflation to a recessionary demand shocks for different degrees of RWRs



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Endogenous participation

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- An increase in the number of participants N<sub>t</sub>↑ makes the labor market looser. A looser labor market exerts a <u>downward pressure</u> on inflation, by reducing hiring costs and by exerting a downward pressure on wages.

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, where  
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firms reservation wage worker's opportunity cost of holding the job A looser labor market reduces both the worker's outside option during the bargaining process (it is more difficult to find a job) and the firm's surplus from an employment relationship (it is easier to replace the worker).

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Why are real wage rigidities irrelevant for inflation, when labor force is endogenous?

• In a downturn, by limiting the downward adjustment of real wages, RWRs entail UPWARD pressures on the marginal cost of production.

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Why are real wage rigidities irrelevant for inflation, when labor force is endogenous?

- In a downturn, by limiting the downward adjustment of real wages, RWRs entail UPWARD pressures on the marginal cost of production.
- But, RWRs make the wage markup countercyclical, and this drives potential workers into the labor market
  - $\longrightarrow$ labor market tightness decreases

 $\longrightarrow$ This additional looseness in the labor market provides <u>DOWNWARD</u> pressures on marginal costs, counterbalancing the upward pressures coming from the standard channel.

• To the extent the recent downturn can be interpreted as demand driven, RWRs should have reduced deflation risks. But the countercyclical profile of LFP, associated with wage rigidities, might have limited the relevance of this standard channel.

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- The assessment of the effects of wage rigidities on inflation cannot disregard the impact that they exert on labor supply.

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  - Wage rigidities, labor force and optimal monetary policy; how monetary policy should differ depending on the cyclical profile of LFP

Family members can be employed, unemployed and searching for a job, or out of the labor force.

U=mass of unemployed; E =mass of employed; L =mass of non-participants

$$\underbrace{U_{t-1} + \rho E_{t-1} + L_{t-1}}_{\text{non-employment pool}} = 1 - (1 - \rho) E_{t-1}$$

 $S_t$ =pool of jobless individuals who are available for hire at the beginning of period t

$$S_t = N_t - (1 - \rho) E_{t-1}$$

$$E_t = (1-\rho) E_{t-1} + f_t S_t$$

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#### Preferences

Go back

- Family members can be employed, unemployed and searching for a job, or out of the labor force. Those who are not participating in the labor force engage in housework, that increases the utility of the whole family
- The household allocates family members between the market and home sectors, on the basis of the relative return to being in either sector, and assigns equal consumption to all members in order to share consumption risk within the family

$$\max \mathbb{E}_{0} \sum_{t=0}^{\infty} \xi_{t} \beta^{t} [\log (C_{t} - hC_{t-1}) - \psi \frac{E_{t}^{1+\varsigma}}{1+\varsigma} + \chi_{t} \frac{(1 - N_{t})^{1-\phi}}{1-\phi}]$$
  
st.
$$\int_{0}^{1} P_{t} (i) C_{t} (i) di + Q_{t} B_{t} \le B_{t-1} + W_{t} E_{t} + T_{t}$$

#### Preferences

• Solving the household's optimization problem we obtain a conventional Euler equation and the participation condition:

$$Q_t = \beta \mathbb{E}_t \frac{\Omega_{t+1}}{\Omega_t} \frac{\xi_{t+1}}{\xi_t} \frac{P_t}{P_{t+1}}$$

$$\underbrace{\frac{\chi(1-N_{t})^{-\phi}}{\Omega_{t}}}_{MRS_{t,L,C}} = f_{t}\underbrace{\left(\frac{W_{t}}{P_{t}} - \underbrace{\psi E_{t}^{\varsigma}}{\Omega_{t}}\right)}_{wage \ markup} + f_{t}\mathbb{E}_{t}\beta\left(1-\rho\right)\frac{\Omega_{t+1}}{\Omega_{t}}\frac{(1-f_{t+1})}{f_{t+1}}MRS_{t+1,L,C}$$

where

$$\Lambda_t = \frac{1}{C_t - hC_{t-1}} - h\beta \mathbb{E}_t \frac{\xi_{t+1}}{\xi_t} \frac{1}{C_{t+1} - hC_t}$$

Two sectors: retail and intermediate firms. Household's members are employed by intermediate firms which face a hiring cost and operate in a competitive market in relation to the goods they produce. Intermediate firms sell their output to retailers, which are monopolistically competitive and set prices in a staggered fashion.

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• A large number of identical, perfectly competitive intermediate firms, indexed by  $j \in [0, 1]$ , and with a technology:

$$X_t(j) = A_t E_t(j)$$

• Firms incur a cost to hire new workers. Vacancies are filled immediately by paying the hiring costs:  $G_t = A_t B f_t^{\eta}$ 

$$\max \mathbb{E}_{t} \sum_{k=0}^{\infty} \beta^{k} \frac{\Omega_{t+k}}{\Omega_{t}} \frac{\xi_{t+k}}{\xi_{t}} \left( \begin{array}{c} \frac{1}{\mu_{t+k}} A_{t+k} E_{t+k}(j) + \\ -\frac{W_{t+k}}{P_{t+k}} E_{t+k}(j) + A_{t+k} B f_{t+k}^{\eta} M_{t+k}(j) \end{array} \right)$$

subject to employment law of motion

$$\frac{1}{\mu_{t}} = \frac{W_{t}}{P_{t}A_{t}} + Bf_{t}^{\eta} - \beta E_{t} \frac{\Omega_{t+1}}{\Omega_{t}} \frac{\xi_{t+1}}{\xi_{t}} \left(1 - \rho\right) \frac{A_{t+1}}{A_{t}} Bf_{t+1}^{\eta} + \mu_{t}^{p}$$

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• A continuum of retailers indexed by  $i \in [0, 1]$ , each producing a differentiated final good. The retail firm purchases the intermediate output on a perfectly competitive market and converts it into a differentiated final good. All retail firms have access to an identical technology

$$Y_t(i) = X_t(i)$$

• Following Calvo (1983), retailers can reset their price at random dates: in each period only a randomly chosen fraction  $(1 - \theta)$  of retailers adjusts their prices. The remaining retailers keep their prices unchanged. The pricing decision of a retail firm obeys the following equilibrium condition:

$$E_t \sum_{k=0}^{\infty} \theta^k \beta^k \frac{\Omega_{t+k}}{\Omega_t} \frac{\xi_{t+k}}{\xi_t} \frac{P_t}{P_{t+k}} Y_{t+k/t} \left( \frac{P_t^*}{P_{t-1}} - \frac{\epsilon}{\epsilon - 1} M C_{t+k/t} \frac{P_{t+k}}{P_{t-1}} \right) = 0$$

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## Wages

The presence of a surplus associated with existing relations implies that many wages may be consistent with equilibrium. We follow Hall (2005), assuming equilibrium wage stickiness:

$$\frac{W_t}{P_t} = \left(\frac{W_{t-1}}{P_{t-1}}\right)^{\gamma} W_t^{r*(1-\gamma)}$$

where  $W_t^{r*}$  is defined as the Nash wage schedule. Nash bargaining satisfies:

$$\mathcal{S}_t^{H} = \vartheta \mathcal{S}_t^{F}$$

 $\mathcal{S}^H_t$ : the household's surplus from an established employment relationship  $\mathcal{S}^F_t$ : denotes the household's and firm's surplus from an established employment relationship

$$\left(W_{t}^{r}\right)^{*} = \frac{\psi E_{t}^{\varsigma}}{\Omega_{t}} + \vartheta A_{t}Bf_{t}^{\eta} - \beta \vartheta E_{t}\frac{\Omega_{t+1}}{\Omega_{t}}\frac{\xi_{t+1}}{\xi_{t}}\left(1-\rho\right)\left(1-f_{t+1}\right)A_{t+1}Bf_{t+1}^{\eta}$$

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$$(W^r_t)^* = b \overline{W}^r_t + (1-b) \underline{W}^r_t$$
  
where  $\underline{W}^r_t$  and  $\overline{W}^r_t$  are defined as follows:

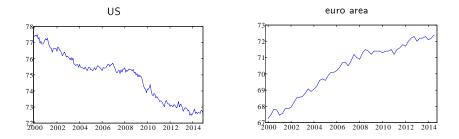
$$\begin{split} \underline{W}_{t}^{r} &\equiv \frac{\psi E_{t}^{\varsigma}}{\Omega_{t}} - \beta \mathbb{E}_{t} \frac{\Omega_{t+1}}{\Omega_{t}} \frac{\xi_{t+1}}{\xi_{t}} \left(1 - \rho\right) \mathcal{S}_{t+1}^{H} + \beta \mathbb{E}_{t} \frac{\Omega_{t+1}}{\Omega_{t}} \frac{\xi_{t+1}}{\xi_{t}} \left(1 - \rho\right) f_{t+1} \mathcal{S}_{t+1}^{H} \\ \overline{W}_{t}^{r} &\equiv \frac{A_{t}}{\mu_{t}} + \beta \mathbb{E}_{t} \frac{\Omega_{t+1}}{\Omega_{t}} \frac{\xi_{t+1}}{\xi_{t}} \left(1 - \rho\right) A_{t+1} \mathcal{B}f_{t+1}^{\eta} \end{split}$$

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$$C_t = A_t (E_t - Bf_t^{\eta} M_t)$$



#### Labor force participation rate, Aged 15-64

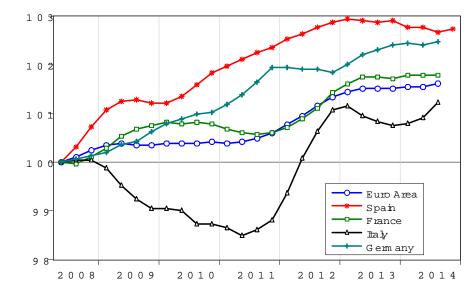




Euro area data refer to the EA-18 aggregate and figures between 2000 and 2004 have been reconstructed by aggregating national data using the

working-age population shares as weights.

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