Optimal Policy for Macro-Financial Stability

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December 7, 2012

Macro-Prudential Policies

• No debate: We need to design policies to deal with financial crises

• Big debate 1: What policy tools should we use?

• Big debate 2: When should policy makers intervene?

 Popular view: Use capital controls as a preemptive intervention to avoid a crisis

• We develop a framework to study optimal policy in and out of crises

 Markov-Perfect optimal policy (no commitment) in a model with an endogenous borrowing constraint

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• Optimality of prudential policy depends on number of instruments

- One instrument: Intervene in a prudential manner
 - True whether a tax on capital or exchange rate intervention
- Two instruments: Intervene when the crisis occurs
- Limited ability of *ex post* policy to mitigate crisis dictates the use of *ex ante* policies
- *Ex ante* policies and capital controls are not needed to implement two "efficient" allocations:
 - Unconstrained allocation
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Preferences

• Households maximize:

$$U\equiv E_0\sum_{t=0}^{\infty}\left\{eta^trac{1}{1-
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• Consumption basket *C* is a composite of tradable and nontradable goods:

$$c_{t} \equiv \left[\omega^{\frac{1}{\kappa}} \left(c_{t}^{T}\right)^{\frac{\kappa-1}{\kappa}} + (1-\omega)^{\frac{1}{\kappa}} \left(c_{t}^{N}\right)^{\frac{\kappa-1}{\kappa}}\right]^{\frac{\Lambda}{\kappa-1}}$$

• Total labor is sum of tradable and nontradable labor supply:

$$h_t = h_t^T + h_t^N$$

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• Access to international capital markets is not only incomplete

$$c_t^T + P_t^N c_t^N + b_{t+1} = \pi_t + W_t h_t + (1+i) b_t,$$

But also imperfect

$$b_{t+1} \ge -\frac{1-\phi}{\phi} \left[\pi_t + W_t h_t\right]$$

 Endogenous prices P^N_t and W_t directly affect constraint, as does individual h_t

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Firms

• Production functions:

$$Y_t^N = A_t^N H_t^{1-\alpha^N}$$
$$Y_t^T = A_t^T H_t^{1-\alpha^T}$$

• Labor demand schedules:

$$W_t = \left(1 - \alpha^N\right) P_t^N A_t^N \left(H_t^N\right)^{-\alpha^N}$$
$$W_t = \left(1 - \alpha^T\right) A_t^T \left(H_t^T\right)^{-\alpha^T}$$

• Dividends to household are residual:

$$\pi_{t} = \alpha^{N} P_{t}^{N} A_{t}^{N} \left(H_{t}^{N} \right)^{1-\alpha^{N}} + \alpha^{T} A_{t}^{T} \left(H_{t}^{T} \right)^{1-\alpha^{T}}$$



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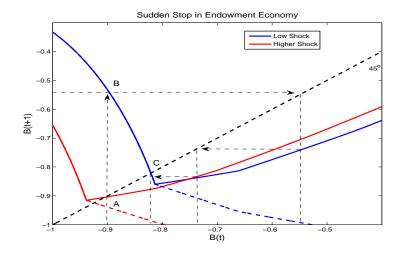
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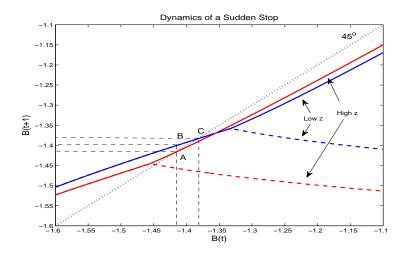
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- Various combinations of taxes:
 - Tax on new debt τ^B (capital control)
 - Tax on nontraded consumption au^N (exchange rate)
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Optimal Policy

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Constraints for Government

• τ_N affects intratemporal allocation between C^T and C^N :

$$(1+\tau_t^N)P_t^N = \frac{(1-\omega)^{\frac{1}{\kappa}} \left(C_t^N\right)^{-\frac{1}{\kappa}}}{\omega^{\frac{1}{\kappa}} \left(C_t^T\right)^{-\frac{1}{\kappa}}}$$

• τ_B affects intertemporal allocation between C^T today and tomorrow:

$$\lambda_{t} = (1 - \tau_{t}^{B})\mu_{t} - \beta (1 + i) E_{t} \left[\mu_{t+1}\right]$$

• Because of pecuniary externality taxation can improve welfare

• Presence of μ_{t+1} in constraint set implies potential time inconsistency, so we look for Markov-perfect equilibrium

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Constraints for Government

• τ_N affects intratemporal allocation between C^T and C^N :

$$(1+\tau_t^N)P_t^N = \frac{(1-\omega)^{\frac{1}{\kappa}} \left(C_t^N\right)^{-\frac{1}{\kappa}}}{\omega^{\frac{1}{\kappa}} \left(C_t^T\right)^{-\frac{1}{\kappa}}}$$

• τ_B affects intertemporal allocation between C^T today and tomorrow:

$$\lambda_{t} = (1 - \tau_{t}^{B})\mu_{t} - \beta (1 + i) E_{t} \left[\mu_{t+1}\right]$$

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Markov-Perfect Equilibrium

A Markov-perfect equilibrium is a value function $V^*(B, A^T)$, government policy functions $\psi_g^*(B, A^T)$, and private sector equilibrium functions $\psi_p^*(B, A^T)$ such that

L Given
$$\widehat{V}(B_{t+1}, A_{t+1}^{T})$$
 and $\widehat{\psi}_{p}(B_{t+1}, A_{t+1}^{T})$, $(\psi_{g}^{*}, \psi_{p}^{*})$ solves

$$\left(\psi_{g}^{*},\psi_{p}^{*}\right)\left(B_{t},A_{t}^{T}\right) = \underset{\psi_{g},\psi_{p}}{\operatorname{argmax}} \left\{ \begin{array}{c} u\left(C\left(\psi_{p},\psi_{g}\right),H\left(\psi_{p},\psi_{g}\right)\right)+\\ \beta E\left[\widehat{V}\left(B'\left(\psi_{p},\psi_{g}\right),A_{t+1}^{T}\right)\right] \end{array} \right\}$$

subject to the equilibrium conditions, and

$$V^* \left(B_t, A_t^T \right) = u \left(C \left(\psi_g^*, \psi_p^* \right), H \left(\psi_g^*, \psi_p^* \right) \right) + \beta E \left[\widehat{V} \left(B' \left(\psi_g^*, \psi_p^* \right), A_{t+1}^T \right) \right];$$

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2 Subgame perfection holds:

$$\widehat{V}\left(B_{t}, A_{t}^{T}\right) = V^{*}\left(B_{t}, A_{t}^{T}\right)$$
$$\widehat{\psi}_{\rho}\left(B_{t}, A_{t}^{T}\right) = \psi_{\rho}^{*}\left(B_{t}, A_{t}^{T}\right).$$

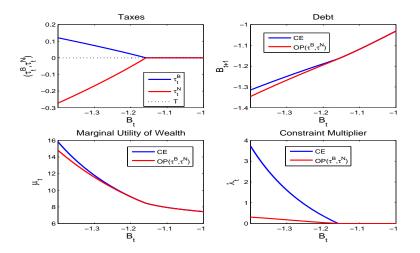
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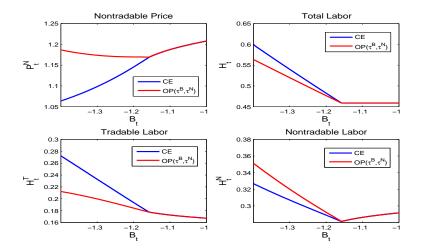


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Optimal Policy



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• With two instruments, only intervene if constraint is binding

- $\bullet\,$ Note that lump-sum tax ${\cal T}$ here is zero, not generally though
- Optimal taxes support nontraded price P^N
- With only one instrument, intervene in opposite directions if constraint is and is not binding

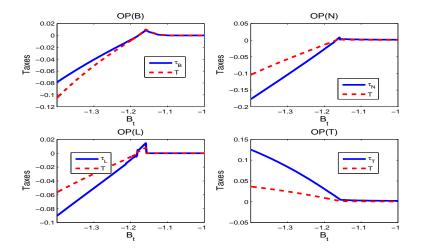
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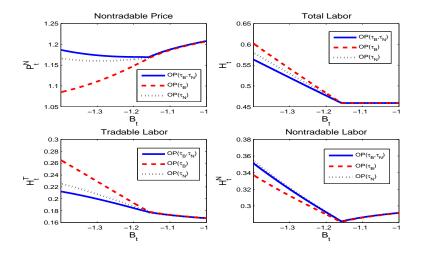


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- Want to study decisions of a planner that internalizes pecuniary externalities
- Wage is required to equal marginal product of labor
- Two possibilities for P^N :

• "Constrained efficient I":

$$P_t^N = \frac{\left(1 - \omega\right)^{\frac{1}{k}} \left(A_t^N \left(H_t^N\right)^{1 - a^N}\right)^{-\frac{1}{k}}}{\omega^{\frac{1}{k}} \left(C_t^T\right)^{-\frac{1}{k}}}$$

• "Constrained efficient II":

$$P_t^N = f^{CE} \left(B_t, A_t^T, A_t^N \right)$$

• We use I here (answers differ)

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Macro-Prudential Policies

- Want to study decisions of a planner that internalizes pecuniary externalities
- Wage is required to equal marginal product of labor
- Two possibilities for P^N :

• "Constrained efficient I":

$$P_t^N = \frac{(1-\omega)^{\frac{1}{\kappa}} \left(A_t^N \left(H_t^N\right)^{1-\alpha^N}\right)^{-\frac{1}{\kappa}}}{\omega^{\frac{1}{\kappa}} \left(C_t^T\right)^{-\frac{1}{\kappa}}}$$

• "Constrained efficient II":

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• Resource constraint on tradables

$$C_t^T = Y_t^T - B_{t+1} + (1+i) B_t$$

• Resource constraint on nontradables

$$C^{N} = Y^{N} = A_{t}^{N} \left(H_{t}^{N} \right)^{1-\alpha^{N}}$$

• Credit constraint

$$B_{t+1} \ge -\frac{1-\phi}{\phi} \left[Y^T + P_t^N Y^N \right]$$

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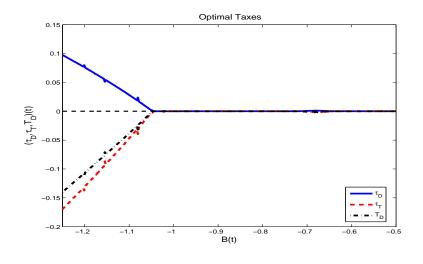
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- Only intervene if constraint is currently binding, tax nontraded sector, subsidize traded sector and profit
- Alternative implementation uses labor income tax instead of lump-sum profit tax

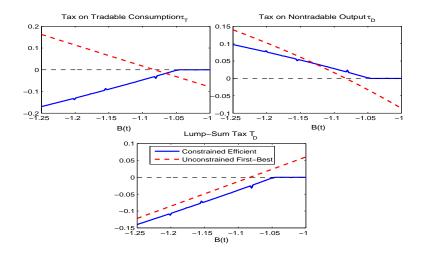
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Implementation of Unconstrained Allocation

- Unconstrained allocation dominates SP (by a lot)
- Government commits to subsidizing nontradables if the constraint binds, resulting in constraint never binding



Implementation of Unconstrained Allocation



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Welfare

Calibration

• Calibrated to Mexico with quarterly data from 1993:1-2007:4

- Evaluated on both business cycle and 1995 Tequila crisis
- Fluctuations are too small, so welfare gains may be lower bound



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Calibration

- Elast. of sub. (tradable and non-tradable goods) $\kappa = 0.76$
- Weight of tradable and non-tradable goods $\omega = 0.32076$
- Utility curvature $\rho = 2$
- Labor supply elasticity $\delta = 1.75$
- Labor share in production $\alpha^T = \alpha^N = 0.66$
- Borrowing constraint 117% of GDP
- Persistence/volatility shock: $\rho_{\tau} = 0.553, \sigma_{T} = 0.028$
- Home real interest rate i = 0.01587
- Unconditional probability of sudden stop 2% per guarter

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Welfare Gains

• Crisis probabilities

CE	SP	ΟΡ(τ _N , τ _B)	ΟΡ(<i>τ_N</i>)	ΟΡ(<i>τ</i> _{<i>B</i>})
1.96	1.63	0.09	0.60	0.00

• Average welfare gains over CE

	Overall	In crisis states
CE	na	na
SP	0.18%	0.22%
ΟΡ(<i>τ</i> _{<i>N</i>} , <i>B</i>)	0.04%	0.05%
$OP(\tau_N)$	0.02%	0.03%
$OP(\tau_B)$	0.003%	0.005%

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Welfare Gains

• Crisis probabilities

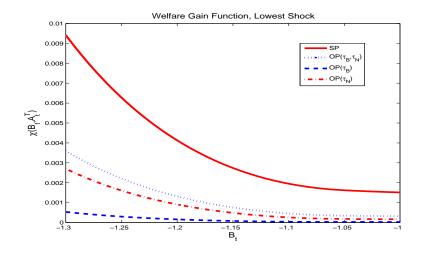
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Welfare Gains



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- Subsidize new debt during crisis, tax it when crisis has positive probability tomorrow
- With sufficient instruments (two), only use *ex post* interventions:
 - Subsidize nontraded sector and tax new debt during crisis, do nothing otherwise
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 - Do not require any ex ante intervention or capital control

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General Lessons

• Ex ante and ex post policy options are jointly determined

• If *ex post* interventions are effective, no need for *ex ante* ones

Less effective "damage control" implies more need for preemptive policy



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