## Inflation, Debt, and Default

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## Motivation



Figure: Inflation and consumption growth co-movement in the U.S.

## The question

How does the inflation process - in particular the co-movement of inflation and consumption growth - jointly affect interest rates, debt dynamics, and debt crises?

## Why does inflation matter?

- The co-movement of inflation and consumption growth affects the risk of nominal debt
$\Rightarrow$ Pro-cyclical inflation makes nominal debt
+ less risky to domestic lender: receives more in bad times
- more risky to domestic borrower: pays out more bad times


## Why does inflation matter?

- The co-movement of inflation and consumption growth affects the risk of nominal debt
$\Rightarrow$ Pro-cyclical inflation makes nominal debt
+ less risky to domestic lender: receives more in bad times
- more risky to domestic borrower: pays out more bad times
- Inflation affects debt pricing
- Debt pricing $\rightarrow$ debt dynamics $\rightarrow$ debt crises $\rightarrow \ldots$


## Further evidence

- Inflation and connection to real yields on government debt
- Compute co-movement of inflation innovations and consumption growth innovations
- OECD 1970-2012 using overlapping windows
- Less pro-cyclical inflation is associated with higher yield


## This paper

- Understand effects of the inflation process on borrowing costs, debt dynamics and debt crises
- Model of sovereign debt
- New ingredients:
- Inflation, exogenous
- Domestic, risk-averse lenders


## Results preview

Co-movement of inflation and consumption growth affects

- Interest rates on debt significant and uniform across states
- Debt dynamics especially during crisis times $\Rightarrow$ risky debt and precautionary motives


## Related literature

- Sovereign default Eaton and Gersovitz (1981), Arellano (2008)
- Domestic default Reinhart and Rogoff (2011), D’Erasmo and Mendoza (2013)
- Default and inflation Aguiar, Amador, Farhi and Gopinath (2012), Sunder-Plassman (2013)
- Cyclicality of inflation

Boudoukh (1993), Ang, Bekaert, and Wei (2008)

- Nominal assets, monetary union and incomplete markets Neumeyer (1998)


## Model

- Builds on standard sovereign debt model (Arellano 2008)
- Government borrows on behalf of domestic poor agents from domestic rich agents
- Both lenders and borrowers risk-averse


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- Government borrows on behalf of domestic poor agents from domestic rich agents
- Both lenders and borrowers risk-averse
- Nominal bonds randomly lose/gain value (exogenous inflation process)


## Model

- Closed economy, discrete time $t=0,1,2, \ldots$, one good
- Endowments $y$ and inflation $\pi$ follow correlated processes
- Agents
- hand-to-mouth households (poor, impatient)
- lenders (high income, patient)
- government
- Government
- borrows from and defaults on domestic lenders, on behalf of poor households, using nominal bonds
- maximizes welfare of poor households


## Government

- Given the option to default, the government chooses

$$
V^{o}(B, y)=\max _{c, d}\left\{V^{c}(B, y), V^{d}(y)\right\}
$$

where $B$ is incoming assets and $y$ is endowment shock

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where $B$ is incoming assets and $y$ is endowment shock

- The value of default is given by

$$
V^{d}(y)=u\left(y^{d e f}\right)+\beta \mathbf{E}_{y^{\prime}}\left[\theta V^{o}\left(0, y^{\prime}\right)+(1-\theta) V^{d}\left(y^{\prime}\right)\right]
$$

where $\theta$ is the probability that the government will regain access to credit markets, $\beta$ the discount factor of the borrower/government, and

$$
y^{d e f}= \begin{cases}\hat{y} & \text { if } y>\hat{y} \\ y & \text { if } y \leq \hat{y}\end{cases}
$$

## Government

- The value, conditional on not defaulting is given by

$$
\begin{aligned}
V^{c}(B, y)= & \max _{B^{\prime}}\left\{U\left(y-q\left(B, y, B^{\prime}\right) B^{\prime}+B\right)\right. \\
& \left.+\beta \mathbf{E}_{y^{\prime}}\left[V^{o}\left(\frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}, y^{\prime}\right)\right]\right\}
\end{aligned}
$$

where $q\left(B, y, B^{\prime}\right)$ is the bond price, $\pi\left(y^{\prime}, y\right)$ is inflation

- Real return on government debt is stochastic (even in absence of default)


## Lenders

- Lenders take as given the policy functions of the government
- Lender's value function is given by

$$
\begin{aligned}
& W(b ; y, s, B)= \max _{b^{\prime}}\left\{u\left(c_{\ell}\right)\right. \\
&\left.+\widehat{\beta} \mathbf{E}_{y^{\prime}, s^{\prime}}\left[W\left(\frac{b^{\prime}}{1+\pi\left(y^{\prime}, y\right)} ; y^{\prime}, s^{\prime}, \frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}\right)\right]\right\} \\
& \text { s.t. } \quad c_{\ell}= \begin{cases}\alpha y+b-q\left(B, y, B^{\prime}(B, y)\right) b^{\prime} & \text { if } s=0 \\
\alpha y^{d e f} & \text { if } s=1\end{cases}
\end{aligned}
$$

where $s=0,1$ denotes the government having access to credit markets, $\widehat{\beta}$ the discount factor of the domestic lender, and $\alpha>1$.

## Pricing kernel

- In this environment, the bond price satisfies

$$
q\left(B, y, B^{\prime}\right)=\mathbf{E}_{y^{\prime}}\left[\frac{1-d\left(\frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}, y^{\prime}\right)}{1+\pi\left(y^{\prime}, y\right)} m_{\ell}\left(y, y^{\prime}, B, B^{\prime}\right)\right]
$$

where

$$
m\left(y, y^{\prime}, B, B^{\prime}\right)=\widehat{\beta} \frac{u^{\prime}\left(c_{\ell}^{*}\left(\frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}, y^{\prime}, B^{*}\left(\frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}, y^{\prime}\right)\right)\right)}{u^{\prime}\left(c_{\ell}^{*}\left(B, y, B^{\prime}\right)\right)}
$$

## Cyclicality of inflation and borrowing costs

- The bond price can be written as

$$
\begin{aligned}
q\left(B, y, B^{\prime}\right)= & \widehat{\beta} \mathbf{E}_{y^{\prime}}\left[\frac{1-d\left(\frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}, y^{\prime}\right)}{1+\pi\left(y^{\prime}, y\right)}\right] \mathbf{E}_{y^{\prime}}\left[\frac{u^{\prime}\left(c_{\ell}^{\prime}\right)}{u^{\prime}\left(c_{\ell}\right)}\right] \\
& +\widehat{\beta} \mathbf{c o v}_{y^{\prime}}\left[\frac{1-d\left(\frac{B^{\prime}}{1+\pi\left(y^{\prime}, y\right)}, y^{\prime}\right)}{1+\pi\left(y^{\prime}, y\right)}, \frac{u^{\prime}\left(c_{\ell}^{\prime}\right)}{u^{\prime}\left(c_{\ell}\right)}\right]
\end{aligned}
$$

- Default and inflation increase borrowing costs; so does countercyclical default (standard effects)
- Pro-cyclical inflation reduces borrowing costs (new channel).


## Cyclicality of inflation and debt dynamics

- Consider the borrower's Euler equation in the absence of default

$$
\begin{aligned}
q\left(B, y, B^{\prime}\right) u^{\prime}(c)= & \beta \mathbf{E}_{y^{\prime}}\left[\frac{1}{1+\pi\left(y^{\prime}, y\right)}\right] \mathbf{E}_{y^{\prime}}\left[u^{\prime}\left(c^{\prime}\right)\right] \\
& +\beta \mathbf{c o v}_{y^{\prime}}\left[\frac{1}{1+\pi\left(y^{\prime}, y\right)}, u^{\prime}\left(c^{\prime}\right)\right]
\end{aligned}
$$

- Pro-cyclical inflation increases incentives to borrow more due to lower borrowing costs (lender's channel)
- However, pro-cyclical inflation also reduces borrower's incentive to take on more debt (riskier asset)


## Quantitative experiment

- In the model with no default, assess impact of different inflation processes on interest rates
- In the full model, assess impact of different inflation processes on interest rates, debt dynamics, and crises


## Functional forms

- Functional forms

$$
\begin{aligned}
u(c) & =\frac{c^{1-\gamma}}{1-\gamma} \\
\log y^{\prime} & =\rho \log y+\varepsilon \text { where } \varepsilon \sim N\left(0, \sigma_{y}^{2}\right)
\end{aligned}
$$

## Functional forms

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$$
\begin{aligned}
& u(c)=\frac{c^{1-\gamma}}{1-\gamma} \\
& \log y^{\prime}=\rho \log y+\varepsilon \text { where } \varepsilon \sim N\left(0, \sigma_{y}^{2}\right) \\
& \pi\left(y^{\prime}, y\right)=\bar{\pi}+\frac{\eta}{v_{y}}\left[\log \left(\frac{y^{\prime}}{y}\right)-\mu_{y}\right] \\
& \text { where } \mu_{y}=\mathbf{E}_{y^{\prime} \mid y}\left[\log \left(\frac{y^{\prime}}{y}\right)\right] \text { and } v_{y}=\operatorname{var}_{y^{\prime} \mid y}\left[\log \left(\frac{y^{\prime}}{y}\right)\right]
\end{aligned}
$$

- This process for inflation satisfies

1. $\mathbf{E}_{y^{\prime} \mid y}\left[\pi\left(y^{\prime}, y\right)\right]=\bar{\pi}$
2. $\operatorname{cov}_{y^{\prime} \mid y}\left[\log \left(\frac{y^{\prime}}{y}\right), \pi\left(y^{\prime}, y\right)\right]=\eta$

## Parameters

| Discount factors | $\beta=0.953$ |
| :--- | :--- |
|  | $\widehat{\beta}=0.983$ |
| Inflation process | $\bar{\pi}=0$ |
|  | $\eta \in\{ \pm 0.0005, \pm 0.0010\}$ |
| Risk aversion | $\gamma=2$ |
| Endowment process | $\rho=0.95, \sigma_{y}=0.02$ |
| Lender endowment | $\alpha \in\{10,100\}$ |
| Probability of re-entry | $\theta=0.282$ |

- We compare borrowing costs and debt dynamics for
$+\eta>0$ (pro-cyclical inflation)
- $\eta<0$ (countercyclical inflation)


## Model with no default

- Borrowing costs are lower with pro-cyclical inflation

Table: Difference in Borrowing Costs

|  | $r_{-\eta}-r_{\eta}$ <br> (in percent) |  |
| :--- | :---: | :---: |
|  | $\eta=0.0005$ | $\eta=0.0010$ |
| $\alpha=10$ | 0.83 | 1.56 |
| $\alpha=100$ | 0.85 | 2.22 |

- The difference is larger with more risk aversion


## Model with default

- Borrowing costs are lower with pro-cyclical inflation
- Yet, debt is also lower with pro-cyclical inflation
- So are default rates

Table: Debt and Default

|  | Positive <br> co-movement <br> $(\eta=+0.0010)$ | Negative <br> co-movement <br> $(\eta=-0.0010)$ |
| :--- | :---: | :---: |
| Default prob. (percent) | 2.52 | 3.04 |
| Spreads (percent) | 2.81 | 3.52 |
| Debt (percent) | 4.29 | 5.48 |

## Inflation and debt dynamics: precautionary motives




## Inflation and debt dynamics: precautionary motives




- Precautionary motives from pro-cyclical inflation increase with debt (i.e. as the borrower gets poorer)
- Meanwhile, lenders uniformly demand lower yield


## Inflation and debt dynamics: a Pyrrhic victory?




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- On average lower rates, debt, and default with pro-cyclicality
- But more volatile rates: riskier debt precisely in bad times


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- On average lower rates, debt, and default with pro-cyclicality
- But more volatile rates: riskier debt precisely in bad times
... a tale of periphery EMU accession?


## Conclusion

- Model of sovereign debt with risk averse domestic lenders and borrowers
- Inflation pro-cyclicality can be important in explaining the observed cross section of government debt, interest rates, and debt crises
- Our findings are relevant for the debate on the costs and benefits of joining a monetary union
appendix


## Conditional co-movement between inflation and consumption growth

- Follow Boudoukh (1993)
- VAR country by country on quarterly data

$$
\left[\begin{array}{l}
\pi_{i t} \\
g_{i t}^{c}
\end{array}\right]=A_{i}\left[\begin{array}{l}
\pi_{i t-1} \\
g_{i t-1}^{c}
\end{array}\right]+\left[\begin{array}{l}
\varepsilon_{\pi i t} \\
\varepsilon_{g i t}
\end{array}\right]
$$

- Compute conditional co-movement between $\varepsilon_{\pi i t}$ and $\varepsilon_{g i t}$ using overlapping five-year windows


## Conditional correlation between inflation and consumption growth



## Inflation cyclicality and real interest rates

Real yield on government debt

|  | (1) | (2) | (3) |
| :---: | :---: | :---: | :---: |
| Inflation co-movement: $\operatorname{cov}\left(\varepsilon_{\pi}, \varepsilon_{g_{c}}\right)$ | $\begin{gathered} -1.379^{* *} \\ (0.576) \end{gathered}$ | $\begin{gathered} -2.007^{* * *} \\ (0.504) \end{gathered}$ | $\begin{gathered} -2.066^{* * *} \\ (0.636) \end{gathered}$ |
| Variance of inflation: $\operatorname{var}\left(\varepsilon_{\pi}\right)$ | $\begin{gathered} 0.418 \\ (0.313) \end{gathered}$ | $\begin{gathered} 0.721^{* * *} \\ (0.222) \end{gathered}$ | $\begin{gathered} 0.211 \\ (0.256) \end{gathered}$ |
| Inflation: $\pi$ | $\begin{gathered} 1.979^{* * *} \\ (0.302) \end{gathered}$ |  | $\begin{gathered} 2.392^{* * *} \\ (0.338) \end{gathered}$ |
| Public debt (percent of GDP) |  | $\begin{aligned} & 0.00281 \\ & (0.0107) \end{aligned}$ | $\begin{gathered} 0.0104 \\ (0.00765) \end{gathered}$ |
| adj. $R^{2}$ | 0.897 | 0.871 | 0.917 |
| $N$ | 2394 | 2049 | 2049 |

Standard errors in parentheses. All regressions include country and year fixed effects.

## Default probabilities




